# **Π** A Brief Introduction to Prime Mechanics

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All work on Prime Mechanics is in the public domain, ad infinitum. Robert T. Turley – Founder/Developer

#### Introduction

One is a number that often goes unnoticed - it's simply there. The heart of the Natural numbers, one is a base unit for so much of the world that this fact may present itself as nothing more than an unconscious thought to most people – a foundation of logic laying the groundwork for a lifetime of conscious and subconscious number pattern recognition. One meter, one second, one person, one sun – a sea of labels.

Add a zero and you have enough data to visualize the binary code inherent to conventional computer systems. Traditionally recognized as a non-value, zero has as much use in applied mathematics as it does in more abstract areas of study such as philosophy, metaphysics and spirituality – alongside its counterpart one.

None of what has been stated should seem far from the ordinary because much of the world relies on the Real Number system, a system that has developed over generations of study and application.



(Source: https://en.wikipedia.org/wiki/Real\_number)

Prime Mechanics does not rely on the Real Number system. In fact, it violates the very division of Rational and Irrational numbers within this system by relying on  $\pi$  as its base value, equating to 'one' in the language's notation. Zero is not a non-value in Prime Mechanics – it is always two Pi.

This short work is an effort to provide the reader with an introductory understanding of Prime Mechanics – its laws, notation, early mapping to Classical Mechanics and a brief outline of the vision behind its development. For a more in-depth look at the early scope of the Axiom project, the reader may visit the project site at www.prime-mechanics.com.

## Classical Mechanics

Classical Mechanics (CM) is defined here as any discipline (field of study or application) that utilizes the Real Number system.

There is a fundamental division within this system – Rational and Irrational numbers. At the heart of the Rational numbers are Natural numbers including one (1), two (2), three (3), etc... Irrationals include values such as π, e and  $\sqrt{2}$ . CM also utilizes the imaginary number *i*, of the expression  $i^2 = -1$ . Zero(0) is used in CM through notation such as binary (Base-2) and decimal (Base-10). Base-60 provides much of the world with a perspective of Time relative to a 24-hour day/night cycle using hours, minutes and seconds. While not all Number Theory relies on these concepts, they are commonplace around most of the modern world (2021, Gregorian calendar).

What is important to note about the categorization of Real Number disciplines as collectively falling under the umbrella of CM is this division of Rational and Irrational. There's a story about Isaac Asimov getting into a debate with his teacher when the teacher breaks a piece of chalk into two, holds up a piece and states that it's half a piece of chalk. Asimov replies by stating that it is, in fact, still one whole piece of chalk. Regardless of which side one may take in this debate, both sides would be considered arguments of CM, which I will explain a bit further on. In essence, we find that conventional mathematics creates a natural division of infinite and finite expression. From Thermodynamics and Electromagnetism to Probability and Uncertainty, this division of 'definable' and 'undefinable' manifests within the logic of the Real Number system itself.

In the next chapter we'll see how Prime Mechanics relies on a fundamentally different logic base than CM, but first we need to look at how CM understands the value Pi. As I mentioned earlier, Pi( $\pi$ ) is considered an Irrational value in CM, whereas one (1) is regarded as the simplest Natural number (some number theorists dispute zero as a Natural number, but as we'll see moving forward the merit of this dispute is irrelevant to the logic base of PM).



In CM, Pi is the fixed ratio of Circumference to Diameter for a unit circle. Two Pi then refers to Tau (τ) the ratio of Circumference to Radius.

We may express the following:

π (Pi) radians = 180° 2π (Tau) radians = 360°

We may also express these values in decimal notation:

 $\pi$  = 3.141... etc. τ = 6.283… etc.

A seemingly trivial observation is that although Tau's ratio is dependent on a value half the size of that which Pi is dependent on (radius versus diameter), its value is twice that of Pi. In the case of rudimentary applications in geometry, Diameter = 2xRadius and Tau = 2xPi are also not mutually exclusive. It is important to note that Pi, when using Real Numbers, may always be given a starting value of 3.

#### Prime Mechanics

Prime Mechanics (PM) is a form of logic that relies on three laws. Two of these three laws violate Classical Mechanics, giving PM a logic foundation distinct from publicly taught and applied mathematics as of 2021.

The name *Prime Mechanics* is derived from the language's use of π as its prime value – the base unit and operator from which the language is structured. We assign π the value 1 in PM, going a step further in written expression by using the character 'I', similar to a capital 'i' or lower-case 'I'. When using PM, we may also refer to  $\pi$  as 'one'.

The Three Laws of PM may be expressed in a number of ways:



While only the second law, two Pi equals Tau, is validated by CM, it is critical to note that the values two and zero are not equivalent in CM – in CM,  $0 = 0$ ,  $2 = 2$ , and  $0 \neq 2$ . Also recall that in CM, the Real Number system states that One and Pi exist as rational and irrational numbers, respectively. By assigning Pi to I and Tau to 0, PM uses logic that requires a different notation and operator in order to develop further.

> III 0 I

I, 0 and III are the simplest forms of Prime notation, which is infinitely expandable using the tally method. I is a more efficient expression of 00, just as 0 is a more efficient expression of II – in both cases, one character is used to represent two. The third value may be expressed in four ways – III, 000, I0 and 0I. This value is of special importance with regards to decimal (Base-10) systems because the number 10 in CM has two values in PM – I and III.

Before going further it's important to understand why the forward-diagonal expression of Prime notation is the most effective. CM relies heavily on the 4-quadrant system (below):



PM only utilizes the first (+,+) quadrant of this system:



While this may seem restrictive at first, using  $\pi$  as the sole operator allows us to navigate this field by providing us with a Primer: [00)[I0)(0I][II]. This Primer follows the III Laws:

$$
II == 0
$$
  

$$
III == 000
$$
  

$$
I == 00
$$

The significance of our third law is that it equates I0 and 0I. By arranging our Primer as it's shown above, we provide a visual aesthetic of the π operator. In earlier works and on the PM site, this operator has also been written as both [3Xx) and [00). [NXx) denotes the I-dimensional (linear) expansion of an initial value – in the case of [3Xx), N = 3. We may express Tau (2Pi) as [6Xx). Where I == 00 is the first law of PM, we may also express the operator  $\pi$  as [00). The bracket notations in both examples reference a ray form, the same form denoted by the Primer:



In the case of our I-dimensional (that is, *pi*-dimensional) line, we have a fixed III-body process correlating to the III laws of PM. In CM there is a different expression for expansion and reduction - in decimal notation for example, we may visualize this expansion and reduction by adding zeros to our base value of 1:

…1,000 , 100 , 10 , 1 , 0.1 , 0.01 , 0.001…

Keep in mind that 10 (ten) does not equal 3 (three) and 1 (one) in CM. It's also important to recognize that values beyond 1 are dependent on 0. While we may express 1 in decimal notation as 1.0, the root of the Natural numbers is not dependent on the non-value 0 in CM.

In Prime notation, these values are simply considered loops of π and τ, reducible to the source,  $I == 00$ :

…I000 , I00 , I0 , I , 0I , 00I , 000I…

By measuring quanta using orders of magnitude such as these, the point of reference may change, but zero remains at the baseline, exemplified in Thermodynamics by the term Absolute Zero (0K = - 273.15°C). PM defines Absolute Zero in its first law, 00 == I, equivocating the thermodynamic state 0K = -273.15°C to π. By integrating all four of the Cartesian quadrants into a single, forward-diagonal plane, PM then establishes a channel for measuring Absolute Zero as a ray [00) rather than a limit, with the Idimensional  $\pi$  as the channel's operator.

Using the III Laws across number groups, we may establish a conversion table for the Base-10 radix (numbers 0-9). This is necessary for understanding how to convert notation relying on Base-10. While CM may utilize a variety of base systems, Prime notation adheres to the III Laws of PM. Since I is always  $π$  and 0 is always τ in PM, these characters have enhanced application over the binary set 1 and 0 (Base-2) in CM.



Our First III Laws establish the Primer:

- 1:  $I == 00$
- $2: 11 == 0$
- $3:$  III == 000

All greater values are simply higher orders of the III Laws, with an increase in the number of folds (binary conversions) as we go higher:

```
4: IIII == 00 == 1
```
- 5:  $\text{III} = 0000 = 1 = 0$
- 6:  $11111 == 000 == 111$
- 7: IIIIIII == 00000 == IIII == 00 == I
- 8:  $1111111 == 0000 == 11 == 0$
- 9: IIIIIIIII == 000000 == III == 000
- 10:  $\text{IIIIIIIII} = 00000 = \text{III} = 00 = 1$
- 11:  $\text{IIIIIIIIII} = 0000000 = 1111 = 00000 = 11 = 0$
- 12: IIIIIIIIIIII == 000000 == III == 000
- 13:  $\text{III}$ IIIIIIIIIII == 00000000 == IIII == 00 == I
- 14: IIIIIIIIIIIIII == 0000000 == IIIII == 0000 == II == 0
- 15: IIIIIIIIIIIIIII == 000000000 == IIIIII == 000 == III
- $16: 11111111111111 = 000000000 = 1111 = 00 = 11$
- 17:  $\text{III}\text{III}\text{III}\text{III}\text{III}\text{III}\text{=}$  = 0000000000 ==  $\text{III}\text{II}\text{III}\text{=}$  0000 ==  $\text{II}\text{I}\text{=}$  0
- 18: IIIIIIIIIIIIIIIIII == 000000000 == IIIIII == 000 == III
- 19: IIIIIIIIIIIIIIIIIII == 00000000000 == IIIIIII == 00000 == IIII == 00 == I
- 20: IIIIIIIIIIIIIIIIIIII == 0000000000 == IIIII == 0000 == II == 0

…

Converting from tallies to the operator notation [00) and writing from bottom-to-top in line with the Primer, our first twenty numbers look like this:

> **Primary** [20)[10)[5)[4)[2)(0] [19)[11)[7)[5)[4)[0)(1] [18)[9)[6)[3)(3] [17)[10)[5)[4)[2)(0] [16)[8)[4)[0)(1] [15)[9)[6)[3)(3] [14)[7)[5)[4)[2)(0] [13)[8)[4)[0)(1] [12)[6)[3)(3] [11)[7)[5)[4)[2)(0] [10)[5)[4)[0)(1] [9)[6)[3)(3] [8)[4)[2)(0] [7)[5)[4)[0)(1] [6)[3)(3] [5)[4)[2)(0] [4)[0)(1] [1)(0] [1)(1] [0)(0]

Note that in this depiction, the third value is  $[1)(0]$  – this may also be expressed as  $[0)(1]$ 

Iterations of 10 are a special case because under Base-10 we recognize that this is a grouping of ten individual units. Using our III Laws, however, we can choose to immediately convert 10 to III or 000, making 10 the first value in Base-10 to have alternate notation (I , III).

The reader may recall that the Primer is ordered I, III, 0 when expressed as a forward-diagonal:





This ordering reveals the loop within Prime notation. To get a better visual of how number values fold within one another using the  $\pi$  operator [00), let's look at the first twenty Natural numbers (left).

Following the conversion provided by our III Laws, we get a defined pattern of I, 0, III. Alternate notation forms its own series of patterns, a fact which provides an alternate method to CM for understanding concepts such as manifolds, dimensions, matrices and other abstract constructs within Number Theory.

It's important to note that we are assigning all starting values the form  $N = πN$ . In other words, any Natural number N is simply a grouping of iterations of π where  $π$ equals one.

By using the notation [Xx) to denote the  $\pi$  operator [00), we establish a method for folding (converting through binary tallying) any Natural number N into one of the Prime values. Our first three are expressed, from bottom to top:



Correlating to the Prime notation:



From this point on, just as with our tally notation, values four (4) and beyond will revert to Prime notation. All values beyond 3 adhere to the following loop:



Recall  $\pi$  as [3Xx) and  $\tau$  as [6Xx) – in this case, D = 2r and Tau = 2Pi are not mutually exclusive, with [6)[3)(3]

expressing both of these statements. 3 = 2(6) is valid because [12Xx) reverts to [3Xx), returning a value of III in Prime notation.

We may then express Pi and Tau in the following terms:

Tau:  $2r = 6$ Pi:  $1D = 3$ 

Twelve as defined by using the  $\pi$  operator [00) gives us:

[12)[6)[3)(3]

Using the value 3 for D (where Pi is [3Xx)) gives us 3, keeping in mind that  $\pi$  as I is equivalent to [00):

 $[3)(3] == [0)(1] == [1)(0]$ 

This equivocation is a result of the non-directional nature of PM where 0 is *not* a non-value, but τ. Since we may also denote  $[0](1)$  as  $[1](0)$ , we have four ways of expressing three values  $(10 == 01 == 111 == 000)$ .

In order to understand how this applies to constructs such as Base-10, let's look at the conversion chart below (recommended zoom at 170% or above):



By understanding that each decimal expansion or reduction of 10 in PM equates to I and III in Prime notation, and that we may assign number values in Base-10 to precise values in Prime notation, we may convert decimal expressions to Prime notation. A much larger sample of the above set is available via the free workbook available on the project site.

The first image below shows a zoomed-out screenshot of  $\pi$  in decimal notation. The second image converts each Base-10 value to its corresponding value in Prime notation, shaded from white to dark grey. Doing so provides a direct method for visualizing number sequences within  $\pi$  by adding a conversion 'filter' to the viewer's perspective.





By understanding iterations of I0 as iterations of  $π$ , Prime notation provides a visual framework for mapping and predicting complex sequences. When using the Base-10 radix conversion, it also allows us to understand number sequences of CM through a different visual and operative aesthetic.



Number values in the above diagram are converted to Prime notation and then color-coded. Let's see how a few well-known number sequences look when converted to this notation.





Alternate Radians and Degrees to Prime notation. Iterations of Pi less than 180 degrees still provide [6)[3)(3].



 $III == 000$ 





In each of the above sequences we are taking a starting value and applying the III Laws through tally notation to reduce that value to Prime notation. Keep in mind that in PM,  $N = \pi N$ , or IN, where N is any Natural number and one equals π. Expressing the operator as [00) provides us with a method for reconverting Prime notation into Natural numbers using the radix converter.

Returning to the story from the previous chapter about Asimov and the chalk, whether we consider the chalk to be one-half of a whole or a whole piece on its own, we are still defining each quantity relative to a base unit of one, the root of the Natural numbers. Standard units allow us to quantify in terms such as 1 meter, 1 second, 1 rotation, 1 sun, 1 table, 1 tree, 1 atom, 1 quark, 1 galaxy – the list is endless, but the governing logic dictates that 1 is not equivalent to π. When we divide three by two in CM, we get one point five  $(3/2 = 1.5)$ . When we subtract five from two, we get negative three  $(2-5 = -3)$ . PM doesn't require partial or negative values because of its equivalence of I to π.

The reason both Asimov and his teacher would have been incorrect within the lens of PM is that in *both* cases, the answer would be  $\pi$  (I) piece of chalk.



Prime notation is being used to understand not only mathematical constants like those above, but physical constants as well. Physical constants such as the gravitational constant and the speed of light are based in Real Numbers, and as such operate within a separate set of logic from PM.

The following page provides an outdated but comprehensive list of physical constants: https://www.nist.gov/system/files/documents/pml/div684/fcdc/wall2014.pdf

By relying on  $\pi$  as a standard unit, operator and primer, PM removes the need for unit conversions. This is why understanding how to map constants to Prime notation is a significant next step in the language's development.

#### Wave Functions

Knowing that PM redefines I and 0 as  $\pi$  and  $\tau$  while integrating the four-quadrant (Cartesian) system into a single forward-diagonal field, let's take a more advanced approach and explore the conventional wave functions of CM.

Consider the cosine (purple), sine (green) and tangent (yellow) curves presented in the four-quadrant system below. In CM we learn that if we were to repeat our iterations of π, these wave functions would also repeat, up to an infinite amount, in opposing directions. That is to say, one may reiterate all three of these trigonometric functions (Sin, Cos, Tan) infinitely to the right or left in the image below.



Using the expression [3Xx) to define the  $\pi$  operator allows us to take concepts within CM and redefine them relative to Prime notation. In the case of Sin, Cos and Tan, these wave functions are conventionally mapped using the four-quadrant system.

To understand these functions in Prime notation, we rotate the quadrants 45 degrees counter-clockwise and reduce the range of the quadrant to I. Higher values are considered redundancies of greater complexity (Entropy), similar to fractal geometry – the Mandelbrot set is featured in many of the earlier works on PM.



PM is non-directional but most efficiently expressed as a forward-diagonal. By factoring in Csc, Sec and Cot, we can define these six functions within the forward-diagonal plane relative to [6Xx), or τ. While the above image depicts a limit of I for both the X and Y axis, the expressions of the Sin, Cos and Tan waves themselves is a current area of interest with respect to the operator [00). Here it becomes a matter of understanding how each curve is re-mapped relative to a single field where  $\pi$  is the sole operator [00), recalling the Primer [00)[I0)(0I][II].



The fractional values of each trigonometric function provide a simple mapping to Prime notation. This table is the latest work in understanding how the fundamentals of CM translate to PM.

In the case of the 6 trigonometric functions (Sin,Cos,Tan and Csc,Sec,Cot) one may recognize that our expressions [3Xx) and [6Xx) provide a rudimentary method for mapping these functions as manifolds of π and  $\tau -$  [6] [3] (3]

Version 1.1 of this intro features an early mapping of Prime notation to these fractional values (left-most column). This early work is experimental and may not represent the most effective form of the notation as the project develops.

### Riemann Hypothesis

Let's take a giant leap now to one of the Millennium Problems of CM, the Riemann hypothesis. The Riemann hypothesis is based on the Riemann-Zeta function, and is defined below in more abstract terms:

"In mathematics, the Riemann hypothesis is a conjecture that the Riemann zeta function has its zeros only at the negative even integers and complex numbers with real part 1/2. Many consider it to be the most important unsolved problem in pure mathematics. It is of great interest in number theory because it implies results about the distribution of prime numbers. It was proposed by Bernhard Riemann (1859), after whom it is named." (https://en.wikipedia.org/wiki/Riemann\_hypothesis)

If we recall from page 18, Prime notation already gives us the ability to understand prime numbers from a fundamentally different perspective. Rather than focusing on the input values themselves, we see them as grouped iterations of the Prime value,  $π$ . Here we must remember that 1 and 0 will always represent  $π$  and  $τ$ .



(https://en.wikipedia.org/wiki/Riemann\_zeta\_function)

Perhaps a simpler way of understanding this function is that depending on the value we plug into the function, ζ(X), the result may be a trivial or non-trivial zero. A trivial zero refers to values lying on the Xaxis to the left of the Y-axis, specifically negative even values (ζ(-2), ζ(-4), ζ(-6)…). The hypothesis states that all *non-trivial* zeros lie on the line X = ½. The image below may help with a visualization:

Polar graph of Riemann zeta( $\frac{1}{2}$  + it)



What is most important to know about the Riemann-Zeta function with respect to PM is that ζ(1) is undefined, or infinite. Knowing that I is  $\pi$  in PM, let's consider the values 0 and  $\frac{1}{2}$ . We may immediately convert 0 to τ, but ½ gives us I/0. Where I0 is both I and III in PM, the line  $X = \frac{1}{2}$  forms a completely different identity within the logic base of PM. Fully converting this function to Prime notation is expected to provide a means for mapping the conventional four-quadrant system to the forwarddiagonal expression of the Primer:



While this paper provides a very brief introduction to how the Riemann hypothesis is understood at face value when using the logic of PM, a workbook is currently available on the project site that provides a much more in-depth mapping of how the notation is converted. For more information the reader may visit the Millennium Problems homepage: https://www.claymath.org/millennium-problems/riemannhypothesis.

An additional page dedicated to this problem is being planned for the Prime Mechanics site as the work progresses. In learning to understand the Riemann Hypothesis, another important expression from CM has been reviewed – Euler's Identity.

#### Euler's Identity – Open Problem

While the Riemann-Zeta function provides a method for understanding how PM defines the zeros of CM, Euler's Identity may present an opportunity to understand how the  $\pi$  operator fully incorporates the irrational field. First let's understand how *e,* eponymously called Euler's Number, is defined:

$$
e=\sum_{n=0}^\infty \frac{1}{n!}=1+\frac{1}{1}+\frac{1}{1\cdot 2}+\frac{1}{1\cdot 2\cdot 3}+\cdots
$$

*e* = 2.71828182845904523536028747135266249775724709369995…



In the above image (source: https://en.wikipedia.org/wiki/E\_(mathematical\_constant), the cutoff *e* gives the shaded surface an area of 1.

Now let's take a look at Euler's Identity:

$$
e^{i\pi}+1=0
$$

As the base of the natural logarithm (ln), *e* may also be expressed as follows:

$$
\ln(e)=1
$$

The open problem asks us to demonstrate, through Prime notation, that the identity  $e^{i\pi} + 1 = 0$ is equivalent to the second law of PM: II == 0.

The identity itself is simple enough that it allows us to convert 1 and 0 to Prime notation immediately:

 $e^{iI} + I = 0$ 

or

 $e^{i\pi} + \pi = \tau$ 

In order to solve for II == 0, we must first state that  $e^{i\pi}$  = I. A deeper understanding of both the trigonometric functions and the Riemann-Zeta function may aid in providing a solution to this problem. For a more detailed explanation of Prime notation and the III Laws, the reader is invited to visit the project site: www.prime-mechanics.com.



#### The Axiom Project

The unoriginally named 'Axiom' project began as the draft for a sci-fi novel, in which a new language for understanding universal phenomena was conceptualized. While I may eventually finish that novel, PM began to take on a life of its own over the years. In the summer of 2020, after almost five years of independent research and development, Prime Mechanics was given its name based on the mapping of the Pi Calendar:



This visualization was the first mapping of the Primer [00)[I0)(0I][II] to one of the most basic expansions in CM, the Inverse-Square Law. By integrating the Periodic Table of Elements into this format with respect to the Primer, the Axiom project hit its first milestone in understanding the value of π as an operator.

#### Closing

Since 2015 all work on this project has been presented within the public domain. The current project vision may be summarized as follows:

--The mapping of Classical Mechanics and its disciplines through Prime notation

--The development of non-zero sum solutions for society in order to establish a more prosperous, collaborative and altruistic global community

--The empowerment of free thinking and free education beyond the influence of Institutional doctrine, supported by the sharing of valued open-source material

In time a separate paper is being considered that would explore the ego bias of Individuals, Cultures and Institutions within a historical and modern context across Abstract and Concrete disciplines. PM will remain open-sourced under the philosophy of free education, global collaboration and equality beyond the restrictions of these ego biases within modern society.